

# FRactal Networks of Carbon Nanopores

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## Introduction

It is well documented in the literature [1,2] that the morphology and, therefore, the adsorptive properties of activated carbons largely depend on the activation process. However, until now, there was no fundamental relation between morphology and activation process [2]. In the present communication, we show, by means of small-angle X-ray scattering (SAXS), that steam activation of a common char yields the formation of a fractal network of nanopores. The existence of a fractal nanopore network may confer to these activated carbons new interesting properties which will be discussed.

## Experimental

The activated carbons (H series) investigated in the present study were prepared [3] from a char obtained from olive stones by carbonization in N<sub>2</sub> at 1123K for 2 hours. The samples were activated under a constant steam flow (100 ml min<sup>-1</sup>) at 1023K. Under these conditions, the activation rate is close to 1% h<sup>-1</sup>. The burn-off (expressed as a weight percentage) is indicated in the sample reference: H0, H8, H22, H37, H52 and H74.

Small-angle X-ray scattering (SAXS) measurements were performed at the Sandia National Laboratories-University of New Mexico Scattering Laboratory in Albuquerque, NM. Data for momentum transfer  $q$  smaller than about 0.03 Å<sup>-1</sup> were measured on a Bonse-Hart scattering system. A pinhole scattering system was used for investigations at larger  $q$  values. The pinhole data were adjusted in intensity to the desmeared Bonse-Hart ones, after corrections for background.

The intensity  $I(q)$  scattered by a fractal surface [4] or by a fractal volume [5] are described by the following power laws:

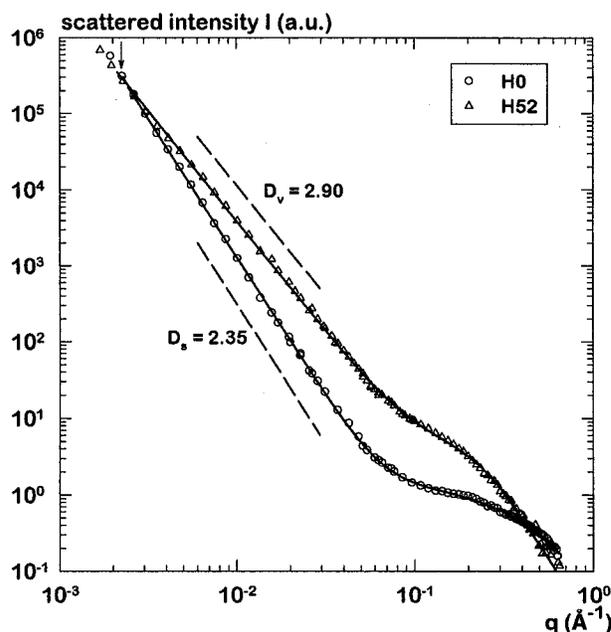
$$I \propto q^{D_s-6} \quad (1)$$

$$I \propto q^{-D_v} \quad (2)$$

in which  $D_s$  and  $D_v$  are respectively surface and volume fractal dimensions.

## Results and Discussion

It was already shown [6] that, in the low- $q$  range, all samples exhibit a surface fractal dimension close to or slightly larger than 2. Thus, this presentation will be focused on the results obtained for  $q$ -values above about 10<sup>-3</sup> Å<sup>-1</sup>. Figure 1 shows the log-log plot of the SAXS data obtained for H0 and H52.



**Figure 1.** SAXS curves obtained for the initial char H0 and the char activated by steam at 52% burn-off (H52). Continuous lines are fits to Eq. 4 and 3b, respectively. The arrow indicates the value of  $q_c$  for H52

A linear regression between a lower limit  $q_c$  and an upper limit close to  $6 \times 10^2$  yields a slope equal to -3.65, in the case of H0. The absolute value of the exponent is larger than 3, inferring from Eq. 1 a surface fractal with  $D_s = 2.35$ . All other samples exhibit volume fractal characteristics (Eq. 2) since the absolute value of the slope range between 2.85 and 2.90 (H37, H52 and H74) or is equal to 3 (H8 and H22). These features are attributed to a fractal pore network. This structure can be modeled [6] as

3-dimensional stacks of 2-dimensional invasion-percolation networks (for which one predicts  $D = 2.89$  [7]) along graphitic planes.

The size  $L_{max}$  of the network is determined from the lower  $q$ -value ( $q = q_c$ ) of the fractal range ( $L_{max} = 2\pi/q_c$ ). The width  $L_{min}$  of the channels belonging to the fractal pore network can be determined from the fit to the data to the following equation:

$$I(q) = K [f(q)]^2 S(q) \quad (3)$$

in which:

- $K$  is a constant for a given system (arbitrary units)
- the form factor is approximated (Guinier approximation) as:  $[f(q)]^2 \cong \exp[-1/5 (qr_1)^2]$ , with  $r_1 = L_{min}/2$
- $S(q)$  is the structure factor, with  $S(q) = 1 + (qr_1)^{-D_v}$  [5]

Thus, Eq. 3 writes:

$$I(q) = I_1 [1 + (qr_1)^{-D_v}] \exp[-1/5 (qr_1)^2] \quad (3a)$$

The three parameters corresponding to the best fit are determined by using the Marquardt-Levenberg algorithm in SigmaPlot® (weight =  $1/[I(q)]^2$ ).

sample	$L_{max}$ (nm)	$L_{min}$ (nm)	$D_v$	$\phi_{SAXS}$	$\phi_{N_2}$	$L_2$ (nm)
H0		0.85	-	-	$\approx 0$	2.02
H8	78	1.64	3	-	0.33	0.78
H22	205	1.38	3	-	0.43	(0.34)
H37	238	1.52	2.87	0.52	0.46	0.84
H52	296	2.12	2.90	0.61	0.51	1.02
H74	343	2.10	2.85	0.47	0.56	0.96

**Table 1.** Parameters obtained from the fit to Eq. (4) for H0 and to Eq. (3b), for activated samples (determination of  $\phi_{SAXS}$  and  $\phi_{N_2}$  is explained in text).

However, it appears that Eq. 3a cannot fit the data up to the largest  $q$ -value. An analytical expression for the whole curve (between  $q_c$  and  $0.66 \text{ \AA}^{-1}$ ) is given by Eq. 3b:

$$I(q) = I_1 [1 + (qr_1)^{-D_v}] \exp[-1/5 (qr_1)^2] + I_2 \exp[-1/5 (qr_2)^2]$$

from which a second family of non correlated objects which scatter independently from the fractal pore network, is inferred. The values of  $D_v$ ,  $L_{min} = 2r_1$  and  $L_2 = 2r_2$ , are collected in Table 1. For  $CO_2$  activated samples, the analysis of  $N_2$  adsorption provided by Monte Carlo simulation [8] shows the existence of two families of micropores, located around 2.4 and 1.2 nm respectively. A similar treatment will allow to decide whether the second family of scattering objects obtained in the present study consists of non-correlated micropores or carbon grains.

By definition, the volume fraction  $\phi_{SAXS}$  of the fractal network is equal to  $(L_{max}/L_{min})^{D_v-3}$ . Even if the second family of scatterers are micropores, its contribution to  $I(q)$  is about ten times smaller than that of the fractal pore

network. Thus, one may compare,  $\phi_{SAXS}$  to  $\phi_{N_2}$  defined as the ratio of the total specific volume of adsorbed nitrogen  $V_{N_2}$  to the total specific volume of the sample  $V_t = V_{N_2} + 1/\rho_{carbon}$  ( $\rho_{carbon} \cong 2 \text{ g/cm}^3$ ). Table 1 shows fair agreement between the two series of values.

The data obtained for the non-activated sample H0, can be fitted to the following equation:

$$I(q) = I_0 q^{D_s-6} + I_1 \exp[-1/5 (qr_1)^2] + I_2 \exp[-1/5 (qr_2)^2] \quad (4)$$

describing the total intensity scattered by three independent scatterers: a fractal surface and two families of non-correlated objects, the first one being likely pores accessible to  $CO_2$  at 273K but not to  $N_2$  at 77K [3].

## Conclusion

Steam activation produces a fractal network of channels with an average channel diameter of 2 nm. By virtue of the high fractal dimension of 2.9 of the network, on length scales of 2-300 nm, the channels criss-cross the solid in a nearly space-filling manner and generate a high porosity of 0.5. Since all the porosity resides in these channels, the solid may be regarded as a matrix of branched carbon nanotubes and may compete with isolated nanotubes, in terms of its potential for gas storage and phase transitions in confined geometries. A distinct advantage of the fractal network is that transport through the branched, interconnected channels is much more rapid than transport in and out of isolated tubes.

## References

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